

## Mössbauer, infrared and X-ray Studies of $\text{Ni}_{0.5}\text{Zn}_{0.5}\text{Cr}_x\text{Fe}_{2-x}\text{O}_4$ ferrites

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Spinel ferrites of the system  $\text{Ni}_{0.5}\text{Zn}_{0.5}\text{Cr}_x\text{Fe}_{2-x}\text{O}_4$ ,  $0 \leq x \leq 1$ , have been studied using the Mössbauer, IR and X-ray patterns. The Mössbauer spectra showed two broad sextets and a central paramagnetic phase. The spectra have been analyzed to two magnetic sites A and B and two quadrupole doublets  $C_A$  and  $C_B$ . Both A and  $C_A$  are assigned to  $\text{Fe}^{3+}$  ions at the tetrahedral A-site, while B and  $C_B$  to  $\text{Fe}^{3+}$  and  $\text{Fe}^{2+}$  representing the octahedral B-site. The obtained hyperfine interaction parameters: the isomer shifts, quadrupole splittings, outermost line widths, hyperfine magnetic fields and bulk magnetization, are discussed as functions of the  $\text{Cr}^{3+}$  content ( $x$ ). The cation distributions of the compounds are estimated using the site preference of the elements and the area ratio of B- to A- sites. Five absorption bands were observed in the infrared spectra in the range between 1100 and 200  $\text{cm}^{-1}$ . The refractive index, the IR velocity in the samples and the jump rate of the lattice vacancies have been determined and discussed as functions of molar ratio ( $x$ ). The Jahn-Teller effect of the  $\text{Fe}^{2+}$ ,  $\text{Ni}^{2+}$  and/or  $\text{Cr}^{4+}$  ions has been observed. From X-ray analysis, the true and theoretical lattice parameters, the oxygen parameter and the ionic radii, bonds, edges and hopping lengths of the A- and B-sites have been calculated and discussed depending on the  $\text{Cr}^{3+}$  ion content ( $x$ ). The hyperfine fields at the A- and B-sites were found to be dependent on the  $\text{Cr}^{3+}$  ion content.

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## 1. Introduction:

Spinel ferrites are still one of the basic materials of modern electronics and computer techniques. Ni-Zn ferrites are attractive for devices of microwave and radio frequency and their applications owing to their high resistivity, mechanical hardness, and high Curie temperature and chemical stability [1-3]. In earlier works some authors, investigated the effect of some additives and substitutions on the physical properties of Ni-Zn ferrites required for high frequency technique [1-3]. It has been found that the main physical properties of spinel ferrites arise from the cationic distribution amongst the tetrahedral A- and octahedral B-sites [4, 5]. The parameters related to the ionic charge and radius, crystal fields play an important role in the site preference of the cations. The effect of  $\text{Cr}^{3+}$  substitution for  $\text{Fe}^{3+}$  in spinel ferrites has been studied extensively [6-8]. The results showed that Cr ions are in the charge state  $\text{Cr}^{3+}$  and intensively occupy the B-sites. When  $\text{Cr}^{3+}$  is progressively replaced by  $\text{Fe}^{3+}$  ions, the crystal structure becomes a cubic spinel structure and its Néel temperature increases. The addition of  $\text{Cr}^{3+}$  ions gives interesting Mössbauer and IR spectra and drastically changes the magnetic hyperfine fields and other Mössbauer, IR and X-ray parameters. Consequently, the aim of the present work is to study the effect of  $\text{Cr}^{3+}$  substitution for  $\text{Fe}^{3+}$  on the physical properties of the spinel system  $\text{Ni}_{0.5}\text{Zn}_{0.5}\text{Cr}_x\text{Fe}_{2-x}\text{O}_4$ ,  $0 \leq x \leq 1$ . The techniques used in this study are the Mössbauer, infrared and X-ray diffraction spectrometers.

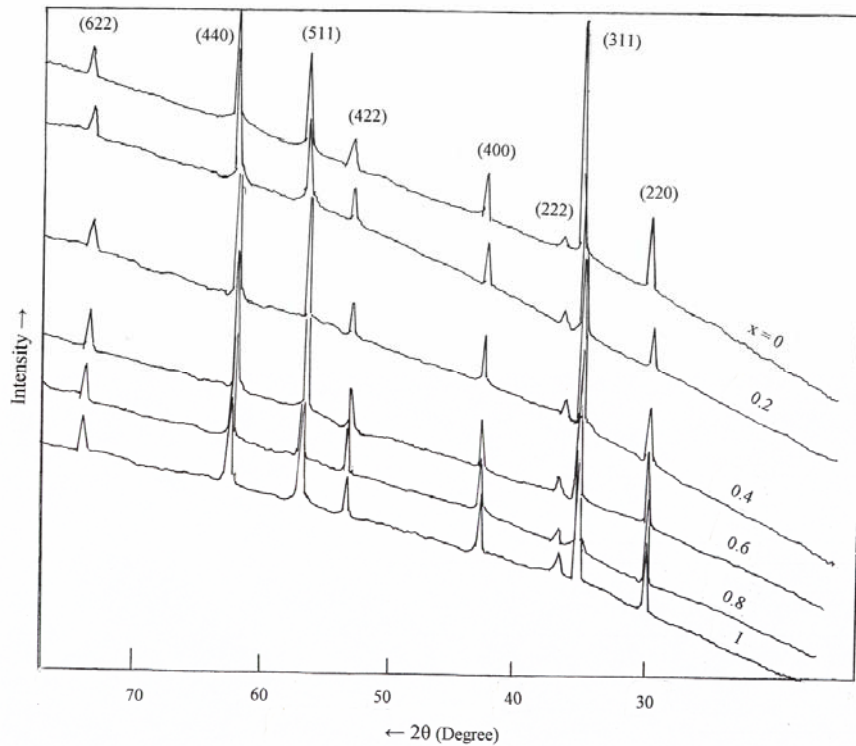
## 2. Experimental:

The spinel samples of the system  $\text{Ni}_{0.5}\text{Zn}_{0.5}\text{Cr}_x\text{Fe}_{2-x}\text{O}_4$ , with  $x = 0, 0.2, 0.4, 0.6, 0.8$  and  $1$ , were prepared by the usual ceramic technique. High purity oxides of NiO, ZnO,  $\text{Cr}_2\text{O}_3$  and  $\text{Fe}_2\text{O}_3$  have been used. The powdered samples were presintered at  $1000^\circ\text{C}$  for one day. Finally the powder samples were pressed into pellets and sintered at  $1200^\circ\text{C}$  for one day and quenched at room temperature in the normal atmosphere.

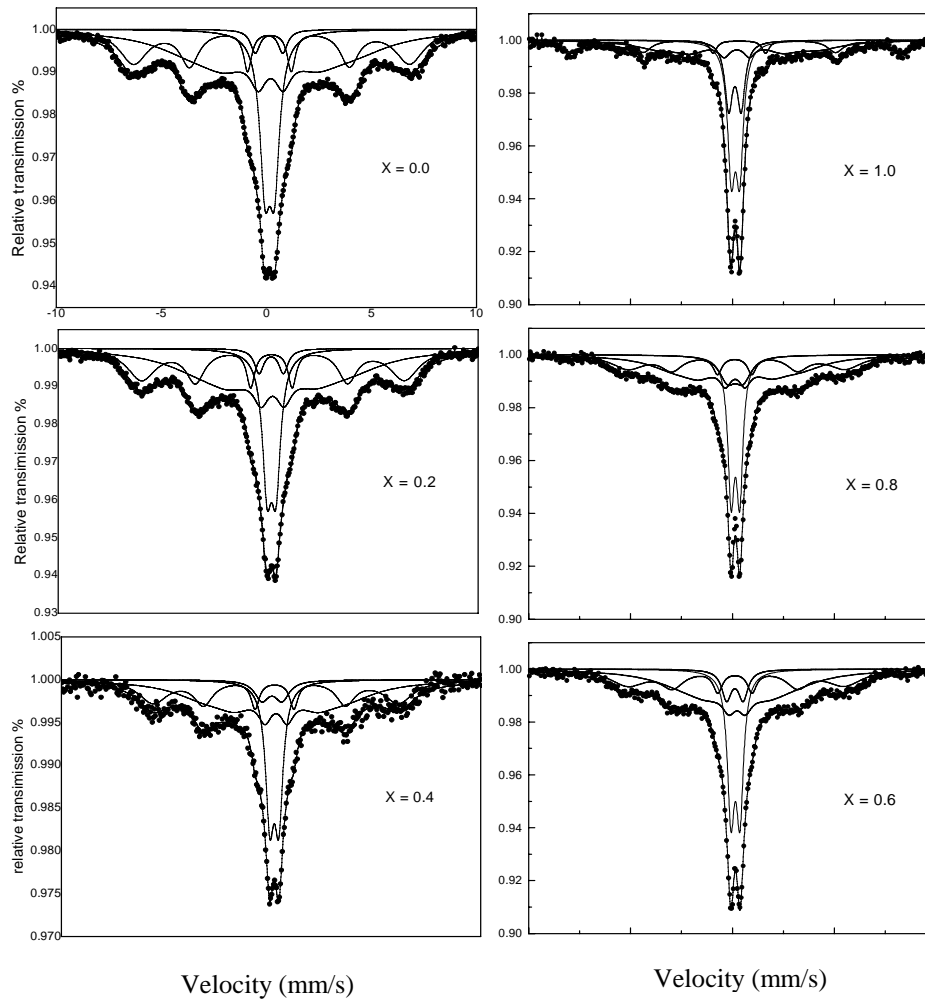
The X-ray diffraction patterns were taken using a Shimadzu X-ray diffractometer XD-3, where a copper  $k_\alpha$  in the X-ray tube target was used. The recorded reflection planes, as shown in Fig. (1), are (220), (311), (222), (400), (422), (511), (440) and (622). Consequently, the appearance of these reflection planes proved that all the prepared samples have cubic spinel structure. The lattice parameter  $a$  was determined as indicated previously [9]. The values of the lattice parameter  $a$  for all samples lie between  $8.359$  and  $8.579 \text{ \AA}$ , and of the interplanar distance  $d$  between  $1.275$  and  $3.025 \text{ \AA}$ , which agree with that obtained previously [6, 9], and ASTM cards.

Figure (2) shows the recorded Mössbauer spectra obtained at room temperature. The Mössbauer spectrometer of the electromechanical type was used in the constant-acceleration mode. The source was  $^{57}\text{Co}$  (up to 50 mCi) in Rh matrix at room temperature, where a metallic iron foil was used for calibration. The spectra were analyzed using the least squares fit computer program. However, two magnetic sextet A and B and two quadrupole doublets  $C_A$  and  $C_B$  could be identified in analyzing the spectra. The sharper magnetic sextet A and the doublet  $C_A$  were assigned to  $\text{Fe}^{3+}$  ions at the tetrahedral A-sites and the broadened sextet B and the doublet  $C_B$  to  $\text{Fe}^{3+}$  and  $\text{Fe}^{2+}$  at the octahedral B-sites.

The infrared absorption spectra were recorded at room temperature using the solid potassium bromide method. The spectra were taken employing a Perkin-Elmer spectrometer in the range from 4000 to 200  $\text{cm}^{-1}$ .



**Fig. (1):** The X-ray diffraction patterns of the  $\text{Ni}_{0.5}\text{Zn}_{0.5}\text{Cr}_x\text{Fe}_{2-x}\text{O}_4$  ferrites.



**Fig. (2):** The Mössbauer spectra of the system  $\text{Ni}_{0.5}\text{Zn}_{0.5}\text{Cr}_x\text{Fe}_{2-x}\text{O}_4$ , obtained at room temperature for the indicated samples.

### 3. Results and Discussion:

#### 3.1. Mössbauer spectra:

Figure (2) shows the room temperature Mössbauer spectra of the  $\text{Ni}_{0.5}\text{Zn}_{0.5}\text{Cr}_x\text{Fe}_{2-x}\text{O}_4$  ferrites. The spectra show a broadened sextet component and a central paramagnetic phase C for all samples. This behaviour is due to statistical fluctuations in the distribution of magnetic and nonmagnetic ions. The phase C arises from those  $\text{Fe}^{3+}$  ions, which are located within regions,

which are so small (particle size) that they behave superparamagnetically [10, 11]. The obtained results from the fits (as two sextets and two doublets) are given in Table (1). It is clear that the paramagnetic phases area of  $C_A$  and  $C_B$  increase with increasing the  $Cr^{3+}$  content  $x$ . This increase may be due to increasing the content of the diamagnetic ions;  $Ni^{3+}$  and  $Cr^{4+}$  in the samples by the fast hopping process;  $Fe^{3+} + Ni^{2+} \leftrightarrow Fe^{2+} + Ni^{3+}$ ,  $Fe^{3+} + Cr^{3+} \leftrightarrow Fe^{2+} + Cr^{4+}$  and/or  $Cr^{4+} + Ni^{2+} \leftrightarrow Cr^{3+} + Ni^{3+}$  [5], where  $Ni^{3+}$  migrates into the A-sites and  $Cr^{4+}$  remains in the B-sites.

**Table (1):** The Mössbauer parameters of the system  $Ni_{0.5}Zn_{0.5}Cr_xFe_{2-x}O_4$ , where  $\epsilon_Q$ ,  $\delta$ ,  $\Gamma_{1,6}$  and  $A_0$  are the quadrupole shift (or the quadrupole doublet splitting), isomer shift, outermost linewidth and fractional area of each (site) subspectrum, respectively.

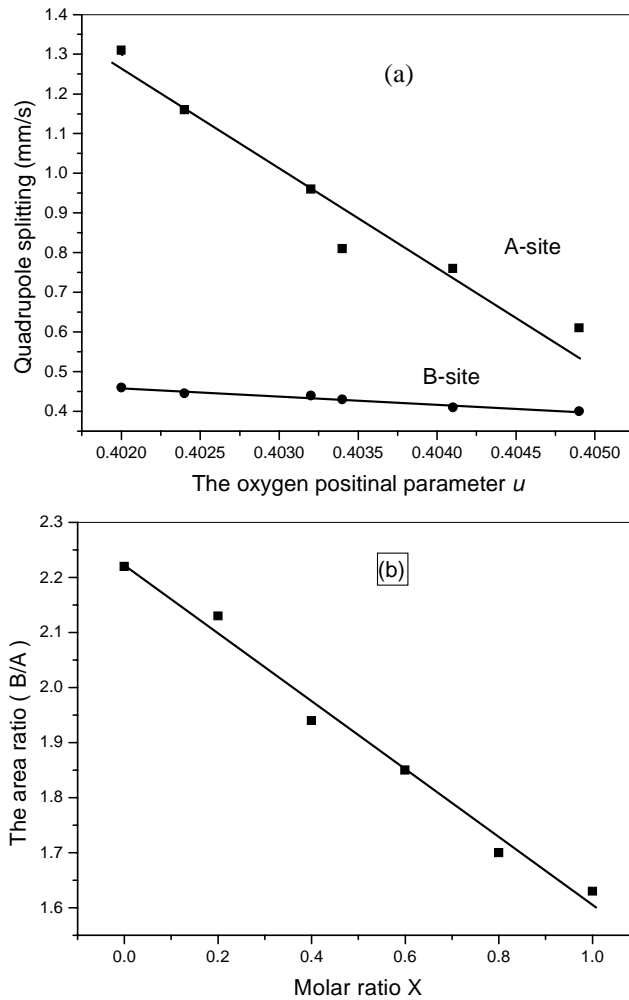
X	Sites	$\epsilon_Q$ (mm/s)	$\delta$ (mm/s)	$\Gamma_{1,6}$ (mm/s)	$A_0$
0	A	0.1	0.19	1.64	0.29
	B	0.11	0.26	4.67	0.49
	$C_A$	1.31	0.13	0.54	0.02
	$C_B$	0.46	0.15	1.11	0.2
0.2	A	0.07	0.19	1.66	0.28
	B	0.14	0.28	4.45	0.47
	$C_A$	1.16	0.14	0.54	0.04
	$C_B$	0.44	0.16	1.01	0.21
0.4	A	0.06	0.2	1.68	0.29
	B	-0.02	0.23	3.71	0.43
	$C_A$	0.96	0.14	0.83	0.05
	$C_B$	0.44	0.15	0.59	0.23
0.6	A	0.06	0.15	2.14	0.27
	B	-0.02	0.22	3.91	0.41
	$C_A$	0.81	0.12	0.57	0.08
	$C_B$	0.43	0.15	0.74	0.24
0.8	A	0.09	0.15	1.96	0.26
	B	0.1	0.18	3.17	0.34
	$C_A$	0.76	0.13	0.97	0.11
	$C_B$	0.41	0.15	0.4	0.29
1	A	-0.13	0.25	1.41	0.20
	B	0.1	0.29	2.93	0.29
	$C_A$	0.61	0.12	0.45	0.18
	$C_B$	0.40	0.15	0.97	0.33
Error		$\pm 0.02$	$\pm 0.02$	$\pm 0.02$	$\pm 0.02$

The isomer shift values  $\delta$  for Fe ions at the A-sites  $\delta_A$  and B-sites  $\delta_B$  (Table 1), lie between 0.13 and 0.29 mm/s, which is consistent with  $\text{Fe}^{3+}$  ions in spinel ferrites [7, 8]. The absolute quadrupole shift values  $\epsilon_Q$  of the magnetic sites A and B,  $\epsilon_{QA}$  and  $\epsilon_{QB}$ , lie between 0.02 and 0.14 mm/s (Table 1). The change of sign may originate from the angular factor [12]. Generally, the  $\epsilon_{QA}$  arises from the asymmetrical charge distribution surrounding  $\text{Fe}^{3+}$  ion and the  $\epsilon_{QB}$  has a trigonal point symmetry and exhibits an electric field gradient EFG along (111) direction. However, the relatively high values of  $\epsilon_{QA}$  and  $\epsilon_{QB}$  may be due to the chemical disorder of the samples, i. e. existing cations of different charges and radii in the sublattices. The relatively high values of  $\delta_B$  and  $\epsilon_{QB}$ , may be due to the mixed valency states between  $\text{Fe}^{2+}$  and  $\text{Fe}^{3+}$  ions.

The doublet structure is due to the quadrupole reaction of  $^{57}\text{Fe}$  nuclei located on the A- and B-sites with EFG at these places. Thus the value of quadrupole doublet splitting  $\epsilon_Q$  can provide information concerning the symmetry of the crystal lattice and its local distortions. The existence of two quadrupole doublets  $C_A$  and  $C_B$ , as shown in Fig. (2), was observed previously [13, 14]. This may arise from the random distribution of cations of different charges and radii on the A- and B-sites, which affects EFG.  $C_A$  and  $C_B$  may result as a consequence of the trigonal distortion of the B-site oxygen coordination i.e. the deformation of the  $3d^5$  shells. This trigonal distortion is confirmed by the high values of the oxygen positional parameter  $u$  (sec 3.3). It is known that the standard value of  $u$  is 0.375 [15], whereas the obtained values are around 0.4. However, the quadrupole splitting values  $\epsilon_Q$  of  $C_A$  and  $C_B$  decrease versus  $x$  (Table 1). This decrease may be due to decreasing the number of  $\text{Fe}^{3+}\text{-O}^{2-}$  bonds, in the sublattices by the substitution process. This may be explained by plotting the relation between both  $\epsilon_{QA}$  and  $\epsilon_{QB}$  and  $u$  as shown in Fig. (3a). This shows that both  $\epsilon_{QA}$  and  $\epsilon_{QB}$  decrease with increasing  $u$ . Hence, an important contribution to EFG arises from  $d$  electron covalence of the  $\text{Fe}^{3+}\text{-O}^{2-}$  bond. As illustrated by the supertransferred hyperfine field, the electrons transfer from the oxygen  $p$  orbitals into the  $\text{Fe}^{3+}$   $d$  orbitals. This transfer causes a slight deformation of the spherical symmetry of the  $3d$  electron charge density, resulting in a significance contribution of the EFG [16]. Consequently, decreasing the number of the  $\text{Fe}^{3+}\text{-O}^{2-}$  bonds decreases the values of  $\epsilon_Q$  at the A- and B-sublattices.

The distribution of  $\text{Fe}^{3+}$  ions amongst the A- and B-sublattices can be understood from plotting the relation between the area ratio of B- to A-site subspectra and (molar ratio)  $x$  as illustrated in Fig. (3b). The decrease of this ratio against  $x$  clears that the substitution process often reduces the  $\text{Fe}^{3+}$  number in the lattice at the expense of the number of  $\text{Fe}^{3+}$  ions at the B-

sublattice. It is well known that the  $Zn^{2+}$  ions exclusively occupy the A-sites [1-6] and the  $Cr^{3+}$  ions the B-sites and the preferred site for the  $Ni^{2+}$  ions is the B-sites [6-8]. Consequently the cation distribution can be estimated, as given in Table (2), using the site preference of elements and the ratio of area under the well resolved subspectra belonging to the A and B sublattices. The outermost line width  $\Gamma_{1,6}$  of the magnetic sites (component) B decreases with  $x$ , whereas that of the magnetic sites (component) A increases for  $x \leq 0.6$  and decreases thereafter (table 1). This may be attributed to the change of the tetrahedral and octahedral environments of the  $Fe^{3+}$  ion at the A- and B-site, i. e. the cations distributions (Table 2).



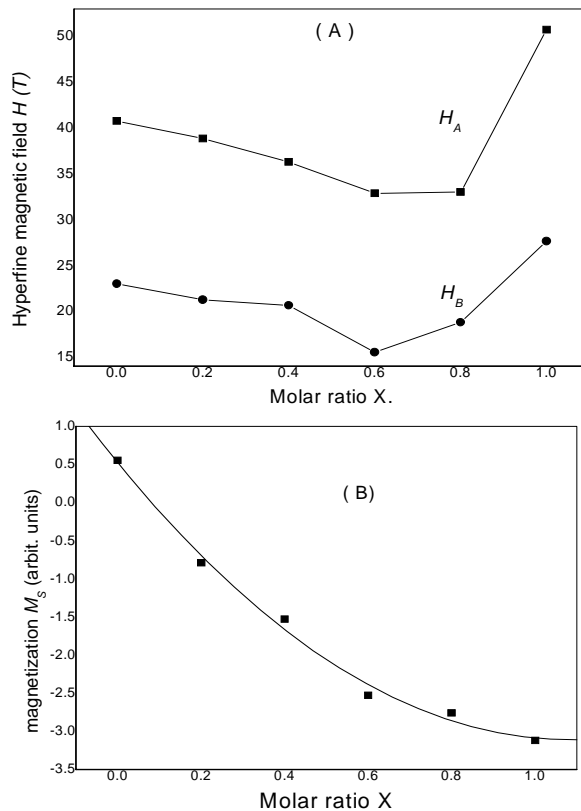
**Fig.(3):** The variation of (a) The quadrupole doublet splitting of the A-sites  $\epsilon_{QA}$  and B-sites  $\epsilon_{QB}$  against the oxygen positional parameter  $u$ , and (b) the area ratio of the B- to the A-site against  $x$ .

The behavior of hyperfine magnetic field  $H$  at A- sites ( $H_A$ ) and B-sites ( $H_B$ ) as functions of  $\text{Cr}^{3+}$  content  $x$  is shown in Fig. (4a).  $H_A$  was found to be greater than  $H_B$ , where they decrease for  $x \leq 0.6$  and increase thereafter. The decrease of  $H_A$  and  $H_B$  can be understood on the basis of decreasing the magnetic superexchange interaction between and within the sublattices due to the reduction of  $\text{Fe}^{3+}$  number. It is necessary to take not only the A-B superexchange but also the B-B supertransferred hyperfine interactions into account. In the cation distribution (Table 2),  $\text{Zn}^{2+}$  ions are non-magnetic and do not contribute to the nuclear magnetic field. Also, the  $\text{Fe}^{3+}\text{-O}^{2-}\text{-Fe}^{3+}$  superexchange interaction is higher than the  $\text{Fe}^{3+}\text{-O}^{2-}\text{-Ni}^{2+}$ ,  $\text{Ni}^{2+}\text{-O}^{2-}\text{-Fe}^{3+}$ , and  $\text{Fe}^{3+}\text{-O}^{2-}\text{-Cr}^{3+}$  [15,17]. As a result,  $H_A$  and  $H_B$  decrease with increasing  $\text{Cr}^{3+}$  content instead of  $\text{Fe}^{3+}$  ions, i. e. decreasing the number of the magnetic bonds  $\text{Fe}^{3+}_A\text{-O}^{2-}\text{-Fe}^{3+}_B$ . Increasing  $H_A$  and  $H_B$ , for  $x \geq 0.8$ , may be attributed, in addition to the magnetic superexchange interactions within the sublattice, to the supertransferred A-A and B-B magnetic hyperfine interactions between the magnetic  $\text{Fe}^{3+}$ ,  $\text{Ni}^{2+}$  and/or  $\text{Cr}^{3+}$  ions inter the A- and B-sublattices. It may arise from a ferromagnetic interaction between the magnetic ions within the sublattice. This increase agrees with that observed previously in Cu-Cr ferrite [6]. The spontaneous magnetization  $M_s$  of the bulk ferrimagnetic material was calculated as stated previously [18, 19]. The calculated negative  $M_s$  Values decrease against  $x$ , as shown in Fig. (4b), indicates that the direction of  $M_s$  is from A to B-sites. The behaviour of  $M_s$  Values against  $x$  is similar to that of Al-ferrites [20].

**Table (2):** Cation distribution in the ferrite system  $\text{Ni}_{0.5}\text{Zn}_{0.5}\text{Cr}_x\text{Fe}_{2-x}\text{O}_4$ .

X	A-site	B-site
0	$\text{Zn}_{0.38}\text{Fe}_{0.62}$	$\text{Zn}_{0.12}\text{Ni}_{0.5}\text{Fe}_{1.38}$
0.2	$\text{Zn}_{0.41}\text{Fe}_{0.59}$	$\text{Zn}_{0.09}\text{Ni}_{0.5}\text{Cr}_{0.2}\text{Fe}_{1.21}$
0.4	$\text{Zn}_{0.46}\text{Fe}_{0.54}$	$\text{Zn}_{0.04}\text{Ni}_{0.5}\text{Cr}_{0.4}\text{Fe}_{1.06}$
0.6	$\text{Zn}_{0.5}\text{Ni}_{0.01}\text{Fe}_{0.49}$	$\text{Ni}_{0.49}\text{Cr}_{0.6}\text{Fe}_{0.91}$
0.8	$\text{Zn}_{0.5}\text{Ni}_{0.06}\text{Fe}_{0.44}$	$\text{Ni}_{0.44}\text{Cr}_{0.8}\text{Fe}_{0.76}$
1	$\text{Zn}_{0.5}\text{Ni}_{0.12}\text{Fe}_{0.38}$	$\text{Ni}_{0.38}\text{Cr}_1\text{Fe}_{0.62}$



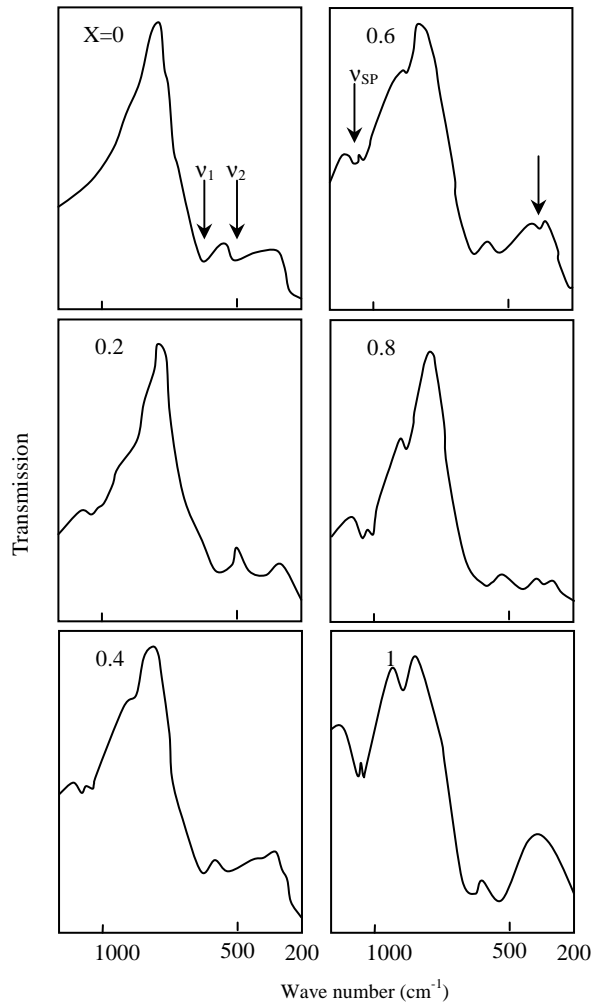


**Fig.(4):** The  $x$  dependence of (a) the hyperfine magnetic field of the A-site  $H_A$  and the B-site  $H_B$  and (b) the calculated spontaneous magnetization  $M_s$ .

### 3.2. Infrared spectra.

The most interesting feature of this study is the IR spectra as shown in Fig. (5). The results of IR studies are listed in Table (3). The two strong absorption bands,  $\nu_1$  and  $\nu_2$  are observed and assigned to the complexes of  $\text{Fe}^{3+}\text{-O}^{2-}$  at the A-site and of  $\text{Fe}^{3+}\text{-O}^{2-}$  and  $\text{Cr}^{3+}\text{-O}^{2-}$  at the B-site vibrational modes [17, 20-23]. The change in band positions is due to the change in the  $\text{Fe}^{3+}\text{-O}^{2-}$  internuclear distances for the A- and B-sites. Fig. (5) and Table (3) clear that the bands  $\nu_1$  and  $\nu_2$  shift towards the high energy with increasing  $\text{Cr}^{3+}$  substitution for  $\text{Fe}^{3+}$  ions. This may be explained on the basis of decreasing the concentration of  $\text{Fe}^{3+}$  ions amongst the A- and B-sites, which cause increasing the metal-oxygen stretching vibrational energies and cause decreasing the B-site ionic radius and reducing the size of the unit cell i.e. the lattice parameter  $a$  (sec. 3.3) [9]. The band  $\nu_3$  results from the splitting of the band  $\nu_2$  by the increasing presence of the  $\text{Fe}^{2+}$  ions at the B-site. Thus the band

$\nu_3$  can be assigned originally to the  $\text{Fe}^{2+}\text{-O}^{2-}$  complexes and to the divalent metal ion-oxygen complexes in the B-sites [19-23]. The intensity of the band  $\nu_3$  increases with increasing  $\text{Cr}^{3+}$  concentration at B-sites due to the increasingly existence of  $\text{Fe}^{2+}$  resulting from the hopping process [5].



**Fig. (5):** The infrared transmittance spectra for the studied samples.

**Table (3):** The absorption band positions  $\nu_n$  and their intensities  $I_n$  ( $n = 0, 1, 2, 3$  and SP), SP denotes to splitting and Sh to Shoulder.

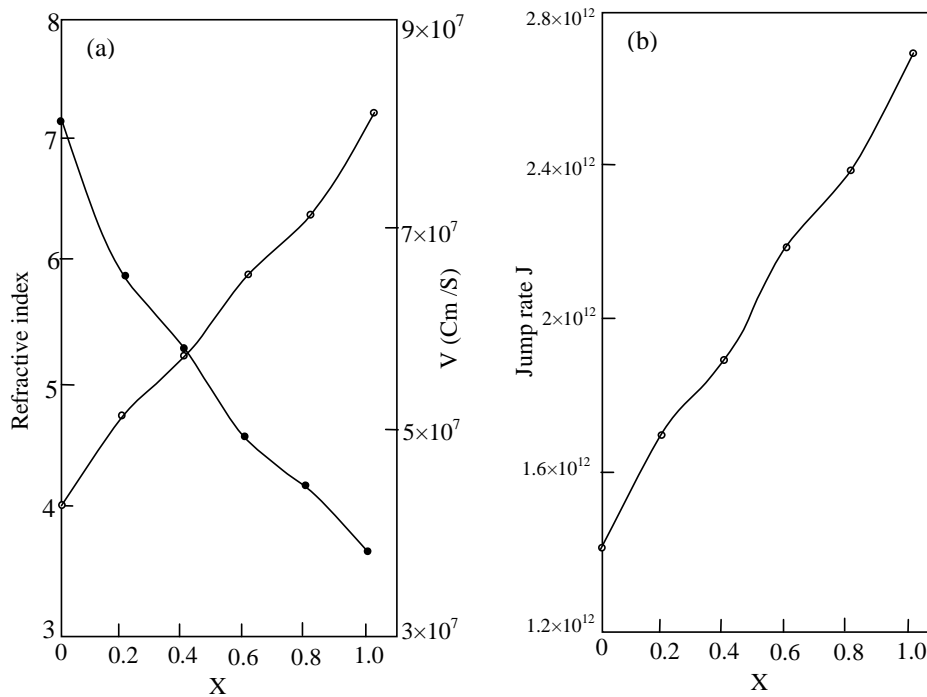
X	$\nu_{SP}$ ( $\text{cm}^{-1}$ )	$I_{SP}$	$\nu_0$ ( $\text{cm}^{-1}$ )	$I_0$	$\nu_1$ ( $\text{cm}^{-1}$ )	$I_1$	$\nu_2$ ( $\text{cm}^{-1}$ )	$I_2$	$\nu_3$ ( $\text{cm}^{-1}$ )	$I_3$
0	-----	---	---	---	577	13	454	14	-----	---
0.2	1084-1043	26	Sh	---	548	13	395	17	-----	---
0.4	1082-1042	43	881	40	585	14	471	19	344	20
0.6	1082-1043	46	880	32	592	15	484	22	340	27
0.8	1082-1041	28	882	63	562	17	438	24	341	29
1	1082-1040	52	880	82	601	21	496	27	342	33
	$\pm 2$	$\pm 2$	$\pm 2$	$\pm 2$	$\pm 2$	$\pm$	$\pm 2$	$\pm$	$\pm 2$	$\pm$
						2		2		2

Two bands  $\nu_0$  and splitting band  $\nu_{SP}$  appeared around  $\nu_1$  and become more pronounced with increasing  $\text{Cr}^{3+}$  ions content (Table 3). The band  $\nu_0$  was observed in the spectra of the Co-Ni ferrites and assigned to the intrinsic vibrations of the tetrahedral group [24, 25]. Some authors [21, 26], using IR and Raman spectra, reported that the peak  $\nu_0$  is generally found very intense in the oxide spinels ( $675 \text{ cm}^{-1}$  in  $\text{Fe}_3\text{O}_4$ ). They assigned it to the breathing mode of the tetrahedral A-sites or to a compound due to distribution of particle morphologies. Two side bands around  $\nu_1$  ( $600 \text{ cm}^{-1}$ ) were found in studying Ni-Zn ferrites [26], and assigned to the presence of  $\text{Fe}^{2+}$  ions in both A- and B-sites. In our case, the two bands  $\nu_0$  and  $\nu_{SP}$  are clearly dependent on the statistical distribution of the cations amongst the A- and B-sites and on the  $\text{Cr}^{3+}$  ion concentration at B-site. The splitting band  $\nu_{SP}$  appeared in studying Co-Zn ferrite [27], and was assigned to the greater concentration of  $\text{Fe}^{2+}$  ions and to the distortion of the spinel lattice. In our system, the band  $\nu_{SP}$  can be assigned to the  $\text{Cr}^{4+}\text{-O}^{2-}$  complexes and to the local distortion of the cubic spinel lattice [26, 27]. Actually the bands  $\nu_3$  and  $\nu_{SP}$  result from the splitting of the band  $\nu_2$  and are characteristic of the Jahn-Teller effect of the ions  $\text{Fe}^{2+}$ ,  $\text{Ni}^{2+}$  and/or  $\text{Cr}^{4+}$  at the B-sites [24]. The intensity of the band  $\nu_{SP}$  increases with increasing chromium addition. This reveals increasing the number of the  $\text{Cr}^{4+}$  ions at the B-sites by the hopping process. The bands  $\nu_0$  results from the splitting of the band  $\nu_1$  by the Jahn-Teller effect of the  $\text{Fe}^{2+}$ ,  $\text{Cr}^{4+}$  and/or  $\text{Ni}^{2+}$  ions at A- sites [24].

The refractive index  $R$  and the velocity  $V$  of the IR waves in the samples can be estimated from the relation [21, 28]:

$$\frac{E_t}{E_{ab}} = \frac{C}{V} = R$$

where  $E_t$  is the transmitted energy,  $E_{ab}$  the absorbed energy and  $C$  the velocity of light. The obtained values of  $R$  and  $V$ , as shown in Fig. (6a), indicate that the refractive index decreases, whereas the velocity of IR increases against  $x$ . The jump rate  $J$  of the lattice vacancies may be estimated from the relation [21, 28]:  $J = \nu e^{E/kT}$ , where  $\nu$  is the frequency of the vibration,  $k$  the Boltzmann constant,  $E = h\nu = V/\lambda$ ,  $h$  is the Planks constant and  $\lambda$  the IR wavelength. Fig. (6b) illustrates that the jump rate  $J$  of the lattice vacancies increase with increasing the  $\text{Cr}^{3+}$  content ( $x$ ). The increase of the absorbed energy at  $\nu_1$  leads to decreasing the refractive index  $R$  with  $x$ . The substitution process  $x$  increases the  $\text{Fe}_A^{3+} - \text{O}^{2-}$  bond length  $d_{AL}$  (table 4) and weakens the B-B superexchange interactions which leads to vibrating the lattice at high frequency with the incident IR waves and to increasing the IR wave velocity  $V$  inside the samples. Increasing the jump rate  $J$  is attributed to increasing the cation vacancies by introducing the smaller  $\text{Cr}^{3+}$  ions into the B-sublattices. It may be attributed to the formation of the larger ions  $\text{Fe}^{2+}$  (0.76 Å) by the hopping process. The formation of larger ions increases the lattice vacancies and increases the jump rate [29].

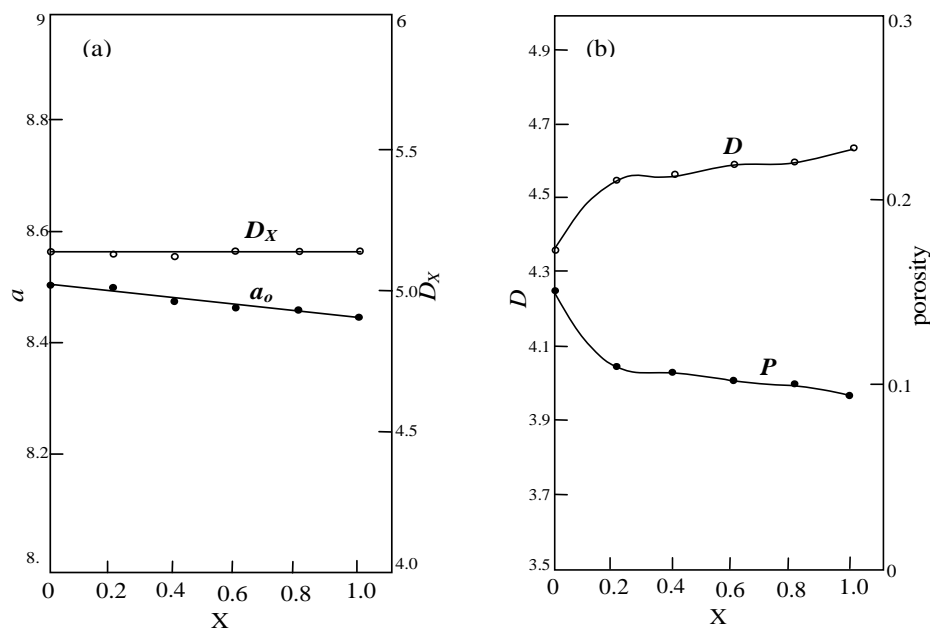


**Fig.(6):** The effect of the  $\text{Cr}^{3+}$  concentration  $x$  on (a) the IR refractive index  $R$  and velocity  $V$ , and (b) the jump rate of the cationic vacancies.

### 3.3. X-ray analysis

The chromium content  $x$  dependence of the theoretical density  $D_x$  is shown in Fig. (7a), and of the bulk density  $D$  and the porosity  $P$  in Fig. (7b). It is shown that  $D_x$  and  $P$  decrease, whereas  $D$  increases with  $x$ . These variations of  $P$  and  $D$  with  $x$  may be attributed to the decrease of the oxygen vacancies, which play a predominant role in accelerating densification [30]. The decrease of  $D_x$  may be assigned to the substitution of the lighter ions  $\text{Cr}^{3+}$  (51.996) instead of  $\text{Fe}^{3+}$  (55.847). For obtaining the true lattice parameter  $a_0$ , the measured lattice parameter  $a$  was plotted versus the Nelson-Riley function [30-32];

$$F(\theta) = \frac{1}{2} \left( \frac{\cos^2 \theta}{\sin \theta} + \frac{\cos^2 \theta}{\theta} \right)$$



**Fig.(7):** The variation of (a) the average lattice parameter  $a_0$  and the theoretical density  $D_x$ , and (b) the bulk density  $D$  and the porosity  $P$ , against  $x$ .

The plots are straight lines with increasing trend, as shown in Fig. (8). The true lattice parameter  $a_0$  can be obtained by extrapolating the lines to  $F(\theta) = 0$  at  $\theta = 90^\circ$ . The obtained values of  $a_0$  are listed in Table (4). The variation of  $a_0$  against  $x$  is shown in Fig (7). a. It is clear that  $a_0$  decreases with increasing the  $\text{Cr}^{3+}$  content in the samples. This decrease is assigned to the

substitution of the smaller radius  $\text{Cr}^{3+}$  ion (0.64 Å) for  $\text{Fe}^{3+}$  ion (0.67 Å). The deduced cation distribution (Table 2) may be confirmed by using it for calculating the theoretical lattice parameter  $a_{\text{th}}$  as indicated previously [33].

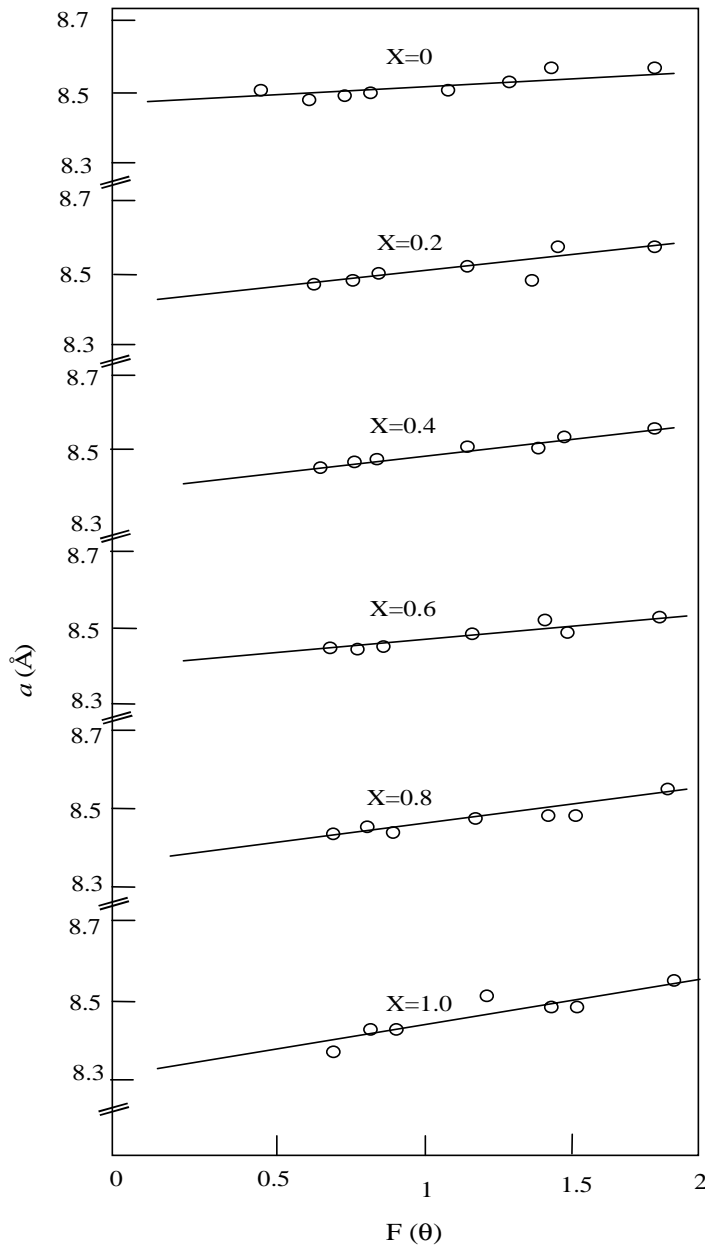


Fig. (8): The relation between Nelson-Riley  $F(\theta)$  and the lattice parameters  $a$ .

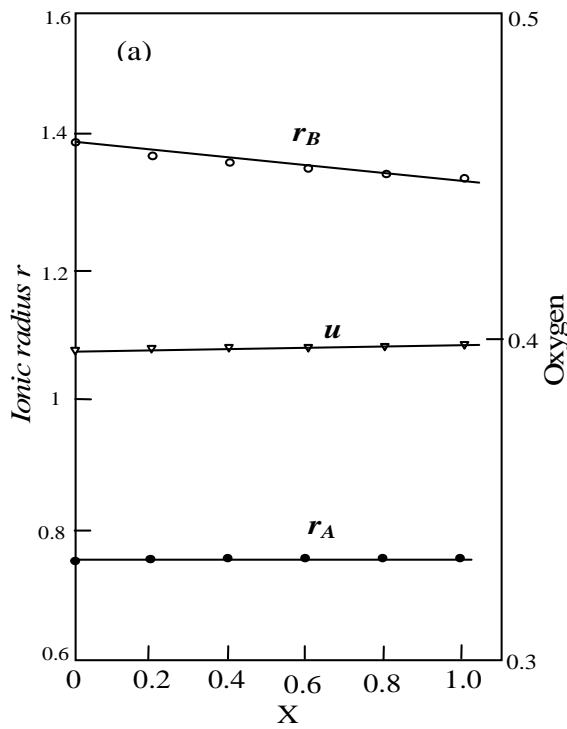
The calculated values of  $a_{th}$  are given in table 4. The comparison between the obtained values for both  $a_0$  and  $a_{th}$  (Table 4) illustrate that their values are approximately equal, which confirm the estimated cation distribution (Table 2). The oxygen parameter  $u$  can be obtained as indicated previously [33-37]. The mean ionic radius of the A-site  $r_A$  and of the B-site  $r_B$  may be calculated as indicated previously [27, 33-37].

**Table (4):** The calculated X-ray parameters; the tetrahedral and octahedral bond length,  $d_{AL}$  and  $d_{BL}$ , the tetrahedral edge  $d_{AE}$ , the shared and unshared octahedral edge  $d_{BE}$  and  $d_{BEU}$  and the true and theoretical lattice parameters  $a_0$  and  $a_{th}$ .

x	$d_{AL}$ (Å)	$d_{BL}$ (Å)	$d_{AE}$ (Å)	$d_{BE}$ (Å)	$d_{BEU}$ (Å)	$a_0$ (Å)	$a_{th}$ (Å)	$L_A$ (Å)	$L_B$ (Å)
0	2.095	1.952	3.421	2.518	2.986	8.4	8.4	3.667	3.006
0.2	2.118	1.939	3.458	2.476	2.987	8.394	8.389	3.642	2.974
0.4	2.147	1.925	3.505	2.428	2.991	8.382	8.378	3.634	2.968
0.6	2.15	1.922	3.51	2.42	2.990	8.384	8.379	3.631	2.965
0.8	2.154	1.92	3.517	2.418	2.991	8.368	8.366	3.623	2.958
1	2.144	1.9	3.492	2.379	2.992	8.334	8.35	3.596	2.936

The calculated values of  $u$ ,  $r_A$  and  $r_B$  are drawn against (molar ratio)  $x$  as shown in Fig. (9a). It is shown that  $r_B$  decreases noticeably as function of  $x$ , whereas  $u$  and  $r_A$  increase slowly. This observation may be due to the correlation between the ionic radius and the lattice parameters [26, 36]. The decrease of  $r_B$  is due to the replacement of the  $Fe^{3+}$  ions at the octahedral B-sites by the smaller radius  $Cr^{3+}$  ions. The increase of  $r_A$  may be due to the increasingly migration of the larger  $Zn^{2+}$  (0.82 Å) and  $Ni^{2+}$  (0.72 Å) to the A-sites (Table 2). The little increase of  $u$  is a direct consequence of increasing the trigonal distortion of the B-site oxygen coordination. Introducing the larger volume  $Zn^{2+}$  and  $Ni^{2+}$  ions into the A-sites increases the trigonal distortion of the B-site oxygen coordination during accommodation these ions.

Using the values of  $a_0$  and  $u$  the tetrahedral and octahedral bond length ( $d_{AL}$  and  $d_{BL}$ ), the tetrahedral edge  $d_{AE}$  and the shared and unshared octahedral edge ( $d_{BE}$  and  $d_{BEU}$ ) may be calculated as indicated previously [33-36]. The calculated values are given in Table 4. It is clear that  $d_{AL}$ ,  $d_{AE}$  and  $d_{BEU}$  increase with  $x$ , which is ascribed to the increasing migration of the larger ions  $Zn^{2+}$  and  $Ni^{2+}$  into the A-sublattices with  $x$  (Table 2). However, the decrease of  $d_{BL}$  and  $d_{BE}$  is attributed to the introducing the smaller radius of the added  $Cr^{3+}$  ions into the B-sites as compared with the substituted  $Fe^{3+}$  ions.

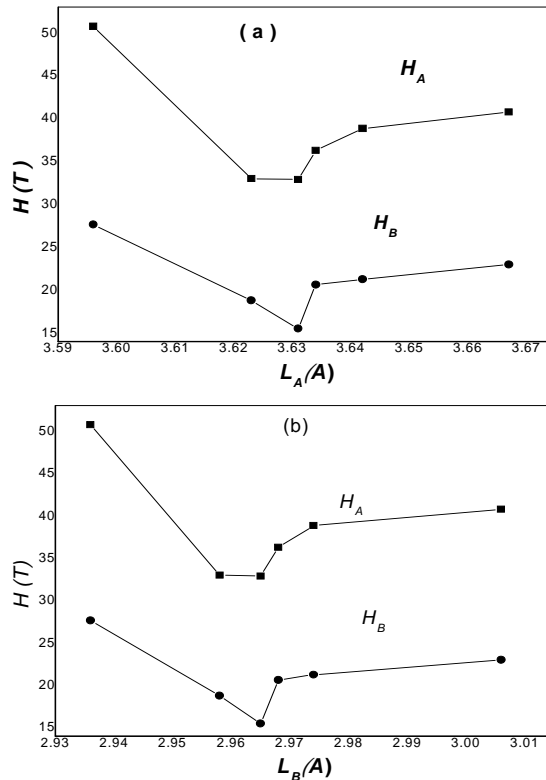


**Fig.(9):** The behaviour of the ionic radius of the A-site  $r_A$  and of the B-site  $r_B$  and the oxygen positional parameter  $u$  as functions of  $x$ .

The distance between the magnetic ions  $L$  (the hopping length) of the A-sites can be obtained by  $L_A = a_0 \sqrt{3} / 4$  and of the B-sites by  $L_B = a_0 \sqrt{2} / 4$  as given in table 4 [36, 38]. Decreasing  $L_A$  and  $L_B$  with  $x$ , as given in Table 4, may be due to reducing the unit cell size ( $a_t$ ). This may be attributed to the introducing of the smaller size magnetic  $\text{Cr}^{3+}$  ions into the B-sublattice and migration the magnetic  $\text{Ni}^{2+}$  ions into the A-sublattices, which make the magnetic ions approach to each other and decrease the hopping length between them. The dependence of the magnetic fields  $H_A$  and  $H_B$  on the hopping lengths  $L_A$  and  $L_B$ , respectively, is shown in Fig (10).  $H_A$  and  $H_B$  reflect the same behavior with  $L$ . Their highest values are at the least distance between the ions, where they decrease sharply to a minimum value for each. This minimum value depends on the distance  $L$  at the corresponding site. However, increasing the distance  $L$  between the site-ions increases the hyperfine field at this site with a slow increasing rate. This may be explained as follows; (1) it is known that the ions  $\text{Ni}^{3+}$  and  $\text{Cr}^{4+}$  are nonmagnetic, the magnetic moment of  $\text{Fe}^{2+}$  ion is less than that of  $\text{Fe}^{3+}$  ion and the hopping



process between the magnetic cations produces  $\text{Ni}^{3+}$ ,  $\text{Cr}^{4+}$  and  $\text{Fe}^{2+}$  ions. (2) Introducing the highest concentration of the smaller  $\text{Cr}^{3+}$  ions (the least  $L$ ) into the B-sublattices creates a cation vacancies, which can block the hopping process between  $\text{Fe}^{3+}$  and  $\text{Ni}^{2+}$ , (3) The high content of  $\text{Cr}^{3+}$  can activate the hopping process between  $\text{Cr}^{3+}$  and both  $\text{Ni}^{3+}$  and  $\text{Fe}^{2+}$  transforming them to  $\text{Ni}^{2+}$  and  $\text{Fe}^{3+}$  ions and giving rise the highest magnetic fields of the sublattices, (4) Hence, decreasing the  $\text{Cr}^{3+}$  concentrations (increasing  $L$ ) increases the hopping process between  $\text{Fe}^{3+}$  and  $\text{Ni}^{2+}$ , therefore  $H_A$  and  $H_B$  decrease to a critical value, (5) above this value the concentration of  $\text{Fe}^{3+}$  ions increase instead of  $\text{Cr}^{3+}$  ions i. e. the number of the magnetic bonds  $\text{Fe}^{3+} - \text{O}^{2-} - \text{Fe}^{3+}$  increase and then  $H_A$  and  $H_B$  increase.



**Fig. (10):** The dependence of the hyperfine fields  $H_A$  and  $H_B$  on the distance between the magnetic ions at the A-sites  $L_A$  and B-sites  $L_B$ , respectively.

#### 4. Conclusion:

X-ray and IR studies proved the spinel structure of the studied system. The Mössbauer spectra have been fitted to two magnetic sextet A and B and two quadrupole doublets  $C_A$  and  $C_B$ . The line widths and the quadrupole doublet splitting of  $C_A$  and  $C_B$  showed a dependency of the  $\text{Cr}^{3+}$  ion content.

Also the  $\text{Cr}^{3+}$  ion contents were found to affect on the area ratio of the B- to A-sites, the hyperfine magnetic field at A- and B-sites,  $H_A$  and  $H_B$ , and the magnetization. The cation distribution has been estimated by X-ray study. The Mössbauer and IR studies reveal the existing of  $\text{Fe}^{2+}$  ions in the sublattices by the hopping process. Five IR absorption bands are reported in the range from 1100 to 200  $\text{cm}^{-1}$ . The additions of  $\text{Cr}^{3+}$  ions change the band positions and shift the bands  $\nu_1$  and  $\nu_2$  towards the high-energy side. The velocity of the IR waves and the jump rate of the lattice vacancies were found to increase, whereas the IR refractive index decreases against (molar ratio)  $x$ . From X-ray studies, the A-site ionic radius, bond length and edge, the B-site unshared edge and the oxygen positional parameter were increasing with increasing  $x$ , whereas the B-site radius, the bond length and shared edge, the hopping lengths, and the true lattice parameter were decreasing. The magnetic fields  $H_A$  and  $H_B$  revealed a dependency on the  $x$  as well as hopping lengths  $L_A$  and  $L_B$  at the A- and B-sites, respectively.

**Note:**

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